

AMATH 483/583

High Performance Scientific Computing

Templates and Generic Programming

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Before

```
class RowMatrix {
public:
    RowMatrix(size_t M, size_t N) : num_rows_(M), num_cols_(N), storage_(num_rows_ * num_cols_) {}

    double& operator()(size_t i, size_t j)      { return storage_[i * num_cols_ + j]; }
    const double& operator()(size_t i, size_t j) const { return storage_[i * num_cols_ + j]; }

    size_t num_rows() const { return num_rows_; }
    size_t num_cols() const { return num_cols_; }

private:
    size_t          num_rows_, num_cols_;
    std::vector<double> storage_;
};
```

After

```
class ColMatrix {
public:
    ColMatrix(size_t M, size_t N) : num_rows_(M), num_cols_(N), storage_(num_rows_ * num_cols_) {}

    double& operator()(size_t i, size_t j)      { return storage_[j * num_rows_ + i]; }
    const double& operator()(size_t i, size_t j) const { return storage_[j * num_rows_ + i]; }

    size_t num_rows() const { return num_rows_; }
    size_t num_cols() const { return num_cols_; }

private:
    size_t          num_rows_, num_cols_;
    std::vector<double> storage_;
};
```

Matrix-Matrix Product

```
Matrix operator*(const Matrix& A, const Matrix& B) {  
    Matrix C(A.num_rows(), B.num_cols());  
    for (size_t i = 0; i < A.num_rows(); ++i) {  
        for (size_t j = 0; j < B.num_cols(); ++j) {  
            for (size_t k = 0; k < A.num_cols(); ++k) {  
                C(i, j) += A(i, k) * B(k, j);  
            }  
        }  
    }  
    return C;  
}
```

```
RowMatrix A(32, 32);  
RowMatrix B(32, 32);  
RowMatrix C = A * B;
```

```
ColMatrix A(32, 32);  
ColMatrix B(32, 32);  
ColMatrix C = A * B;
```

Matrix-Matrix Product

```
RowMatrix operator*(const RowMatrix& A, const RowMatrix& B) {  
    RowMatrix C(A.num_rows(), B.num_cols());  
    for (size_t i = 0; i < A.num_rows(); ++i) {  
        for (size_t j = 0; j < B.num_cols(); ++j) {  
            for (size_t k = 0; k < A.num_cols(); ++k) {  
                C(i, j) += A(i, k) * B(k, j);  
            }  
        }  
    }  
    return C;  
}
```

```
RowMatrix A(32, 32);  
RowMatrix B(32, 32);  
RowMatrix C = A * B;
```

Why should we
ever write more
than one?

Matrix-matrix
product is the same
for any matrix

```
ColMatrix operator*(const ColMatrix& A, const ColMatrix& B) {  
    ColMatrix C(A.num_rows(), B.num_cols());  
    for (size_t i = 0; i < A.num_rows(); ++i) {  
        for (size_t j = 0; j < B.num_cols(); ++j) {  
            for (size_t k = 0; k < A.num_cols(); ++k) {  
                C(i, j) += A(i, k) * B(k, j);  
            }  
        }  
    }  
    return C;  
}
```

```
ColMatrix A(32, 32);  
ColMatrix B(32, 32);  
ColMatrix C = A * B;
```

What's wrong with
writing more than
one?

A programming problem

- “I’ve assigned this problem in courses at Bell Labs and IBM. Professional programmers had a couple of hours to convert the description into a programming language of their choice; a high-level pseudo code was fine... Ninety percent of the programmers found bugs in their programs (and I wasn’t always convinced of the correctness of the code in which no bugs were found).”

- Jon Bentley, Programming Pearls, 1986

This must be a
complicated
algorithm!

Binary search solution

```
int* lower_bound(int* first, int* last, int x)
{
    while (first != last)
    {
        int* middle = first + (last - first) / 2;

        if (*middle < x) first = middle + 1;
        else last = middle;
    }

    return first;
}
```

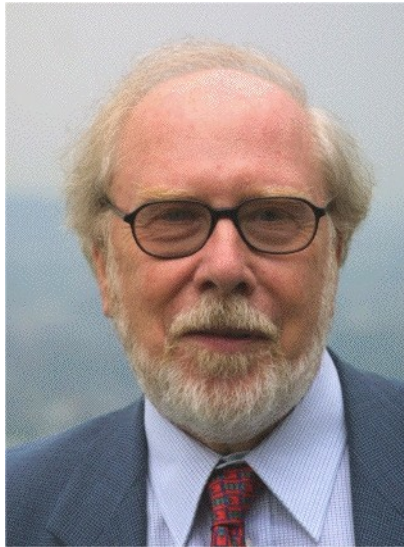
If We Can't Write Binary Search...

- Jon Bentley's solution is considerably more complicated (and slower)
- Photoshop uses this problem as a take home test for candidates.
 - > 90% of candidates fail.
- Experience teaching algorithms indicate that > 90% of engineers, regardless of experience, cannot write this simple code

- It's about correctness

Let an expert write binary search

- Once and for all



Matrix-Matrix Product

```
template <typename MatrixType>
MatrixType operator*(const MatrixType& A, const MatrixType& B) {
    MatrixType C(A.num_rows(), B.num_cols());
    for (size_t i = 0; i < A.num_rows(); ++i) {
        for (size_t j = 0; j < B.num_cols(); ++j) {
            for (size_t k = 0; k < A.num_cols(); ++k) {
                C(i, j) += A(i, k) * B(k, j);
            }
        }
    }
    return C;
}
```

This will work for any type that meets requirements for MatrixType

Constructor
Accessor

```
NewMatrix A(32, 32);
NewMatrix B(32, 32);
NewMatrix C = A * B;
```

```
RowMatrix A(32, 32);
RowMatrix B(32, 32);
RowMatrix C = A * B;
```

```
ColMatrix A(32, 32);
ColMatrix B(32, 32);
ColMatrix C = A * B;
```

```
Matrix A(32, 32);
Matrix B(32, 32);
Matrix C = A * B;
```

Generic Programming Methodology

1. Study the concrete implementations of an algorithm
2. **Lift** away unnecessary requirements to produce a more abstract algorithm
 - a) Catalog these requirements.
 - b) Bundle requirements into **concepts**.
3. Repeat the lifting process until we have obtained a generic algorithm that:
 - a) Instantiates to efficient concrete implementations.
 - b) Captures the essence of the “higher truth” of that algorithm.

Lifting

Array of doubles

Beginning

End

Overload (ad-hoc polymorphism)

```
double sum(double* x, size_t N) {  
    double s = 0;  
    for (size_t i = 0; i < N; ++i)  
        s += x[i];  
    return s;  
}
```

```
double* dx;  
size_t dN;  
double dz = sum(dx, dN);
```

Array of floats

Beginning

End

Overload (ad-hoc polymorphism)

```
float sum(float* x, size_t N) {  
    float s = 0;  
    for (size_t i = 0; i < N; ++i)  
        s += x[i];  
    return s;  
}
```

```
float* fx;  
size_t fN;  
float fz = sum(fx, fN);
```

But we need a different implementation for every type

Polymorphism: same function can be called with different types

Lifting

Array of Ts

Beginning

End

Parametric polymorphism

```
template <typename T>
T sum(T* x, size_t N) {
    T s = 0;
    for (size_t i = 0; i < N; ++i)
        s += x[i];
    return s;
}
```

```
double* dx;
size_t dN;
double dz = sum(dx, dN);

float* fx;
size_t fN;
float fz = sum(fx, fN);
```

Polymorphism not
due to overload,
rather parameterized
by argument type

Parametric
polymorphism

Polymorphism: same
function can be called
with different types

Before

```
double sum(double* x, size_t N) {  
    double s = 0;  
    for (size_t i = 0; i < N; ++i)  
        s += x[i];  
    return s;  
}
```

Before

```
float sum(float* x, size_t N) {  
    float s = 0;  
    for (size_t i = 0; i < N; ++i)  
        s += x[i];  
    return s;  
}
```

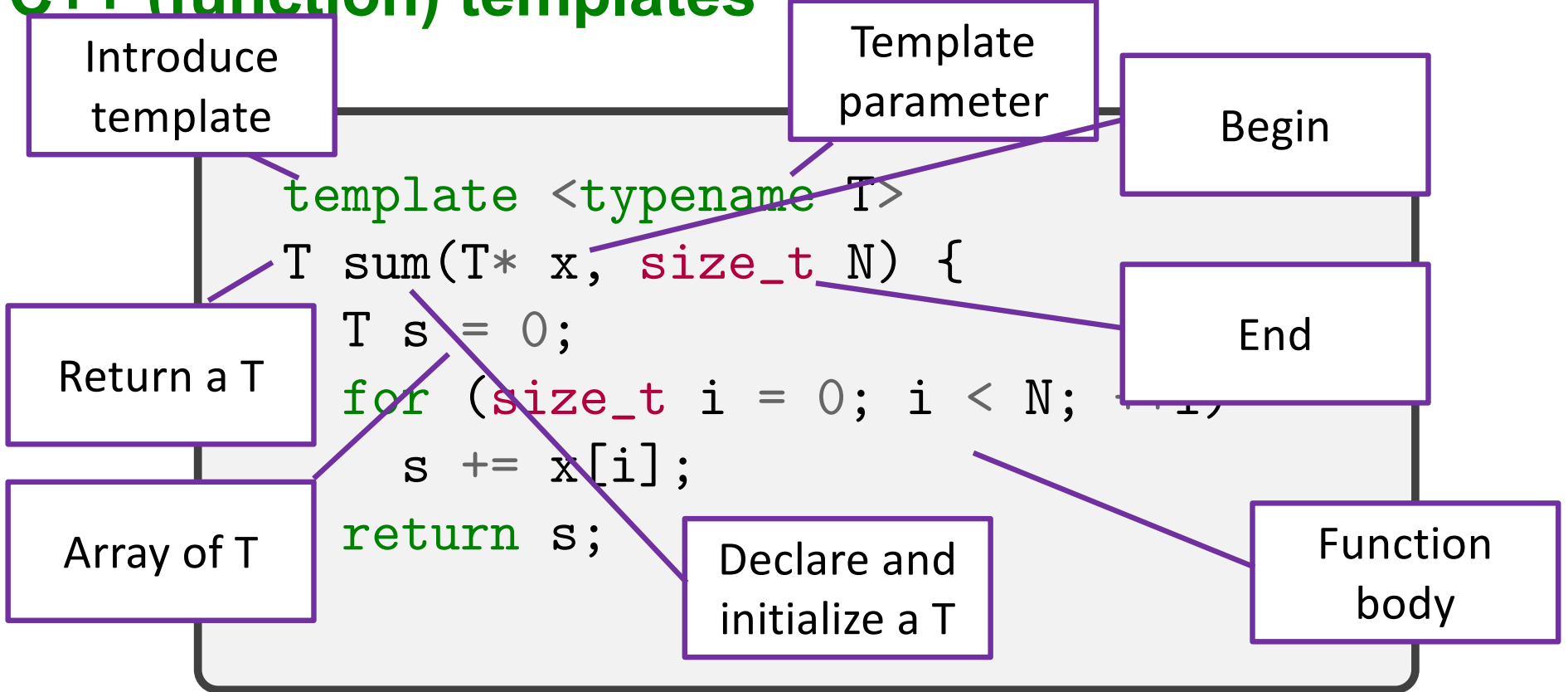
Exactly the
same loop

After

```
template <typename T>
T sum(T* x, size_t N) {
    T s = 0;
    for (size_t i = 0; i < N; ++i)
        s += x[i];
    return s;
}
```

Exactly the
same loop

C++ (function) templates



C++ (function) templates

```
template <typename T>
T sum(T* x, size_t N) {
    T s = 0;
    for (size_t i = 0; i < N; ++i)
        s += x[i];
    return s;
}
```

The function gets created on instantiation

```
double* dx;
size_t dN;
double dz = sum<double>(dx, dN);
```

```
float* dx;
size_t dN;
float dz = sum<float>(dx, dN);
```

This is not a function

It is a function template

A blueprint for a function

C++ (function) templates

```
template <typename T>
T sum(T* x, size_t N) {
    T s = 0;
    for (size_t i = 0; i < N; ++i)
        s += x[i];
    return s;
}
```

At this level

Bind T to be a double

```
double* dx;
size_t dN;
double dz = sum<double>(dx, dN);
```

At this level

```
float* dx;
size_t dN;
float dz = sum<float>(dx, dN);
```

Bind T to be a float

But we know this is a float

C++ (function) templates

```
template <typename T>
T sum(T* x, size_t N)
{
    T s = 0;
    for (size_t i = 0; i < N; ++i)
        s += x[i];
    return s;
}
```

At this level

```
double* dx;
size_t dN;
double dz = sum(dx, dN);
```

Bind T to be a double

```
float* dx;
size_t dN;
float dz = sum(dx, dN);
```

Bind T to be a float

C++ (function) templates

```
int main() {  
  
    Vector v(1024);  
    double a = sum(v, v.num_rows());  
  
    return 0;  
}
```

Bind T to be a
Vector

```
template <typename T>  
T sum(T* x, size_t N) {  
    T s = 0;  
    for (size_t i = 0; i < N; ++i)  
        s += x[i];  
    return s;  
}
```

```
$ c++ vector_sum.cpp  
vector_sum.cpp:16:14: error: no matching function for call to 'sum'  
    double a = sum(v, v.num_rows());  
                  ^~~  
vector_sum.cpp:4:3: note: candidate template ignored: could not match 'T *' against 'Vector'  
T sum (T* x, size_t N) {  
  ^  
1 error generated.
```

C++ (function) templates

```
int main() {
```

```
    Vector v(1024);
```

```
    double a = sum(&v[0], v.num_rows());
```

```
    return 0;
```

```
}
```

Bind T to be a
double*

```
template <typename T>
T sum(T* x, size_t N) {
    T s = 0;
    for (size_t i = 0; i < N; ++i)
        s += x[i];
    return s;
}
```

C++ (function) templates

```
struct element {
    double val;
    element* next;
};

int main() {
    size_t N = 0;
    element* linked_list = null;

    // create list
    double a = sum(linked_list, N);

    return 0;
}
```

Bind T to be an
element*

```
template <typename T>
T sum(T* x, size_t N) {
    T s = 0;
    for (size_t i = 0; i < N; ++i)
        s += x[i];
    return s;
}
```

```
$ g++ linked_list_0.cpp
linked_list_0.cpp:22:10: error: no viable conversion from 'element' to 'double'
    double a = sum(linked_list, N);
               ^
linked_list_0.cpp:5:5: error: no viable conversion from 'int' to 'element'
    T s = 0;
    ^
linked_list_0.cpp:22:14: note: in instantiation of function template specialization 'sum<element*>' requested here
    double a = sum(linked_list, N);
                   ^
linked_list_0.cpp:12:8: note: candidate constructor (the implicit copy constructor) not viable: no known conversion from 'int' to 'const element &' for 1st argument
struct element {
    ^
linked_list_0.cpp:9:10: error: no viable conversion from returned value of type 'int' to function return type 'element'
    return 0;
    ^
linked_list_0.cpp:12:8: note: candidate constructor (the implicit copy constructor) not viable: no known conversion from 'int' to 'const element &' for 1st argument
struct element {
    ^
3 errors generated.
```

Requirements for sum

We need to be able to assign 0 to a T

Pointer to an array of T

Something that can count Ts

```
template <typename T>
T sum(T* x, size_t N) {
    T s = 0;
    for (size_t i = 0; i < N; ++i)
        s += x[i];
    return s;
}
```

But what if I want to sum over a linked list?

We need to index into the array

Perfectly reasonable

Template for sum so far

We have a thing we want to sum over

Beginning of the thing

End of the thing

```
template <typename T>
T sum(T* x, size_t N) {
    T s = 0;
    for (size_t i = 0; i < N; ++i)
        s += x[i];
    return s;
}
```

The type of s can be set to zero

Go through the thing

Get a value out of the thing

The value is not the same as the thing

The value of the thing can be added to s

The value is not the same as the thing

Lifting

```
template <typename T>
T sum (T* begin, T* end) {
    T s = 0;
    for (T* p = begin; p < end; ++p) {
        s += *p;
    }
    return s;
}
```

We don't know what kind of thing, so parameterize

From begin to end

Use pointer

Dereference pointer

Get a value

OK for linked list?

Almost, actually

Lifting

```
template <typename T>
T sum (T* begin, T* end) {
    T s = 0;
    for (T* p = begin; p < end; ++p) {
        s += *p;
    }
    return s;
}
```

Get value

Go to next element

Linked list can do this

Lifting

begin

```
template <typename T>
T sum (T* begin, T* end) {
    T s = 0;
    for (T* p = begin; p < end; ++p) {
        s += *p;
    }
    return s;
}
```

```
double sum(element* x) {
    double s = 0;
    while (x != nullptr) {
        s += x->val;
        x = x->next;
    }
    return s;
}
```

Get value

Go to next
element

end

We can do all the
things needed for sum

But we can't use
it with our sum

Because of syntax

For your consideration (Element son)

Element
"thing"

```
struct element_ptr {  
    element_ptr(element* x) : x(x) {}  
    element_ptr operator++() { x = x->next; return x; }  
    element_ptr operator++(int) { element* y = x; x = x->next; return y; }  
    double operator*() { return x->val; }  
    bool operator==(element_ptr y) { return x == y.x; }  
    bool operator!=(element_ptr y) { return x != y.x; }  
  
    element* x;  
};
```

We also need to
compare

Get value

Go to next

Lifting

Get value

```
template <typename T>
T sum (T* begin, T* end) {
    T s = 0;
    for (T* p = begin; p < end; ++p) {
        s += *p;
    }
    return s;
}
```

No less than

Check

Move to
next

```
struct element_ptr {
    element_ptr(element* x) : x(x) {}
    element_ptr operator++() { x = x->next; return x; }
    element_ptr operator++(int) { element* y = x; x = x->next; return y; }
    double operator*() { return x->val; }
    bool operator==(element_ptr y) { return x == y.x; }
    bool operator!=(element_ptr y) { return x != y.x; }
};
```

element* x;

};

Check

Lifting

Get value

Compare for equality

```
template <typename T>
T sum (T begin, T end) {
    T s = 0;
    for (T p = begin; p != end; ++p) {
        s += *p;
    }
    return s;
}
```

Check

Wrong type
for s

Move to
next

Will s be
compatible
with "0"

```
struct element_ptr {
    element_ptr(element* x) :
    element_ptr operator++() { return x; }
    element_ptr operator++(int) { element* y = x; x = x->next; return y; }
    double operator*() { return x->val; }
    bool operator==(element_ptr y) { return x == y.x; }
    bool operator!=(element_ptr y) { return x != y.x; }
};
```

Check

Check

Lifting

Rename
some things

```
template <typename Iter, typename T>
T sum (Iter begin, Iter end, T init) {
    for (T p = begin; p != end; ++p) {
        init += *p;
    }
    return init;
}
```

And pass in
initial value
of s

Parameterize
the type of s

```
struct element_ptr {
    element_ptr(element* x) : x(x) {}
    element_ptr operator++() { x = x->next; return x; }
    element_ptr operator++(int) { element* y = x; x = x->next; return y; }
    double operator*() { return x->val; }
    bool operator==(element_ptr y) { return x == y.x; }
    bool operator!=(element_ptr y) { return x != y.x; }

    element* x;
};
```


Final

Lets us iterate through our thing

The thing is holding values of type T

```
template <typename ForwardIterator, typename T>
T sum(ForwardIterator begin, ForwardIterator end, T init) {
    while (begin != end)
        init += *begin++;
    return init;
}
```

Use iterators to mark begin and end of what we want to sum

Compare

Get value

Move to next

Add to init

Requirements

```
template <typename ForwardIterator, typename T>
T sum(ForwardIterator begin, ForwardIterator end, T init) {
    while (begin != end)
        init += *begin++;
    return init;
}
```

If the type we bind to ForwardIterator has these expressions, we can use sum

- Need dereference – `*i`
- Need increment – `i++`
- Need equality comparison – `i == j` (equiv `i != j`)

Lifting

```
template <typename ForwardIterator, typename T>
T sum(ForwardIterator begin, ForwardIterator end, T init) {
    while (begin != end)
        init += *begin++;
    return init;
}
```

```
double dd = sum(dx, dx + dN, 0.0);
double ff = sum(fx, fx + fN, 0.0);
double ll = sum(lx, nullptr, 0.0);
```

Specialization

```
double dd = sum(dx, dx + dN, 0.0);  
double ff = sum(fx, fx + fN, 0.0);  
double ll = sum(lx, nullptr, 0.0);
```

```
double sum(double* x, size_t N) {  
    double s = 0;  
    for (size_t i = 0; i < N; ++i)  
        s += x[i];  
    return s;  
}
```

```
float sum(float* x, size_t N) {  
    float s = 0;  
    for (size_t i = 0; i < N; ++i)  
        s += x[i];  
    return s;  
}
```

```
double sum(element* x) {  
    double s = 0;  
    while (x != nullptr) {  
        s += x->val;  
        x = x->next;  
    }  
    return s;  
}
```

Instantiation model

- Instantiation model— For each template instance, a separate piece of code is generated, and compiled.
- Not directly required by the standard, but all language rules assume it. Used by every C++ compiler (except for Lunar).
- Different from Generic Java, Eiffel, ... which compile generic definitions to a single skeleton code.
- Speed/space trade-off: instantiation model often faster, but prone to code bloat.
- Some evidence suggest otherwise (Mark Jones, Haskell dictionary passing).

Unconstrained genericity

```
template <typename ForwardIterator, type  
T sum(ForwardIterator begin, ForwardIterator end, T init) {  
    while (begin != end)  
        init += *begin++;  
    return init;  
}
```

Even though we have a spec for this

How much of this can we type check (and when)?

```
double dd = sum(dx, dx + dN, 0.0);  
double ff = sum(fx, fx + fN, 0.0);  
double ll = sum(lx, nullptr, 0.0);
```

For each template instance, a separate piece of code is generated, and compiled

Unconstrained genericity

- Maximal reusability (structural conformance). Concise: no need to express constraints.
- No separate type checking, error diagnostics must be delayed until instantiation.
- Errors may occur deep inside a generic library. Errors difficult to interpret, difficult to assign blame.

Error messages

```
#include <iostream>
#include <algorithm>
#include <iterator>
#include <vector>
class A {};

int main() {
    std::vector<A> a;
    // ...
    std::copy(a.begin(), a.end(),
        ↪ std::ostream_iterator<A>(std::cout,
        ↪ "\n"));
}
```


Error messages

```
/usr/include/c++/3.2/bits/stream_iterator.h: In member function
  'std::ostream_iterator<_Tp, _CharT, _Traits>& std::ostream_iterator<_Tp,
  _CharT, _Traits>::operator=(const _Tp&) [with _Tp = A, _CharT = char,
  _Traits = std::char_traits<char>]':
/usr/include/c++/3.2/bits/stl_algobase.h:241:
  instantiated from ' _OutputIter std::__copy(_RandomAccessIter,
  _RandomAccessIter, _OutputIter, std::random_access_iterator_tag)
  [with _RandomAccessIter = A*, _OutputIter =
  std::ostream_iterator<A, char, std::char_traits<char> >] '
/usr/include/c++/3.2/bits/stl_algobase.h:260: instantiated from
  ' _OutputIter std::__copy_aux2(_InputIter, _InputIter, _OutputIter,
  __false_type) [with _InputIter = A*, _OutputIter =
  std::ostream_iterator<A, char, std::char_traits<char> >] '
/usr/include/c++/3.2/bits/stl_algobase.h:303: instantiated from
  ' _OutputIter std::__copy_ni2(_InputIter, _InputIter, _OutputIter,
  __false_type) [with _InputIter = A*, _OutputIter =
  std::ostream_iterator<A, char, std::char_traits<char> >] '
/usr/include/c++/3.2/bits/stl_algobase.h:314: instantiated from
  ' _OutputIter std::__copy_ni1(_InputIter, _InputIter, _OutputIter,
  __true_type) [with _InputIter = __gnu_cxx::__normal_iterator<A*,
  std::vector<A, std::allocator<A> > >, _OutputIter =
  std::ostream_iterator<A, char, std::char_traits<char> >] '
/usr/include/c++/3.2/bits/stl_algobase.h:349: instantiated from
  ' _OutputIter std::copy(_InputIter, _InputIter, _OutputIter) [with
  _InputIter = __gnu_cxx::__normal_iterator<A*, std::vector<A,
  std::allocator<A> > >, _OutputIter = std::ostream_iterator<A, char,
  std::char_traits<char> >] ' cpp_templates/cpp_templates.w:1067:
  instantiated from here
/usr/include/c++/3.2/bits/stream_iterator.h:141: no match for '
  std::basic_ostream<char, std::char_traits<char> >& << const A&'
  operator
```

Error messages

```
/usr/include/c++/3.2/bits/ostream.tcc:55: candidates are:
std::basic_ostream<CharT, _Traits>& std::basic_ostream<CharT,
_Traits>::operator<<(std::basic_ostream<CharT,
_Traits>&*) (std::basic_ostream<CharT, _Traits>&*) [with _CharT =
char, _Traits = std::char_traits<char>]
/usr/include/c++/3.2/bits/ostream.tcc:77:
std::basic_ostream<CharT, _Traits>& std::basic_ostream<CharT,
_Traits>::operator<<(std::basic_ios<CharT, _Traits>&*) [with _CharT =
char, _Traits = std::char_traits<char>]
/usr/include/c++/3.2/bits/ostream.tcc:99:
std::basic_ostream<CharT, _Traits>& std::basic_ostream<CharT,
_Traits>::operator<<(std::ios_base&*) (std::ios_base&*) [with
_CharT = char, _Traits = std::char_traits<char>]
/usr/include/c++/3.2/bits/ostream.tcc:171:
std::basic_ostream<CharT, _Traits>& std::basic_ostream<CharT,
_Traits>::operator<<(long int) [with _CharT = char, _Traits =
std::char_traits<char>] /usr/include/c++/3.2/bits/ostream.tcc:208:
std::basic_ostream<CharT, _Traits>& std::basic_ostream<CharT,
_Traits>::operator<<(long unsigned int) [with _CharT = char,
_Traits = std::char_traits<char>]
/usr/include/c++/3.2/bits/ostream.tcc:146:
std::basic_ostream<CharT, _Traits>& std::basic_ostream<CharT,
_Traits>::operator<<(bool) [with _CharT = char, _Traits =
std::char_traits<char>] /usr/include/c++/3.2/ostream:104:
std::basic_ostream<CharT, _Traits>& std::basic_ostream<CharT,
_Traits>::operator<<(short int) [with _CharT = char, _Traits =
std::char_traits<char>] /usr/include/c++/3.2/ostream:118:
std::basic_ostream<CharT, _Traits>& std::basic_ostream<CharT,
_Traits>::operator<<(short unsigned int) [with _CharT = char,
_Traits = std::char_traits<char>] /usr/include/c++/3.2/ostream:119:
std::basic_ostream<CharT, _Traits>& std::basic_ostream<CharT,
_Traits>::operator<<(int) [with _CharT = char, _Traits =
std::char_traits<char>] /usr/include/c++/3.2/ostream:130:
std::basic_ostream<CharT, _Traits>& std::basic_ostream<CharT,
_Traits>::operator<<(unsigned int) [with _CharT = char, _Traits =
std::char_traits<char>] /usr/include/c++/3.2/bits/ostream.tcc:234:
std::basic_ostream<CharT, _Traits>& std::basic_ostream<CharT,
_Traits>::operator<<(long long int) [with _CharT = char, _Traits =
std::char_traits<char>] /usr/include/c++/3.2/bits/ostream.tcc:272:
std::basic_ostream<CharT, _Traits>& std::basic_ostream<CharT,
_Traits>::operator<<(long long unsigned int) [with _CharT = char,
_Traits = std::char_traits<char>]
/usr/include/c++/3.2/bits/ostream.tcc:298:
std::basic_ostream<CharT, _Traits>& std::basic_ostream<CharT,
_Traits>::operator<<(double) [with _CharT = char, _Traits =
std::char_traits<char>] /usr/include/c++/3.2/ostream:145:
std::basic_ostream<CharT, _Traits>& std::basic_ostream<CharT,
_Traits>::operator<<(float) [with _CharT = char, _Traits =
std::char_traits<char>] /usr/include/c++/3.2/bits/ostream.tcc:323:
std::basic_ostream<CharT, _Traits>& std::basic_ostream<CharT,
_Traits>::operator<<(long double) [with _CharT = char, _Traits =
std::char_traits<char>] /usr/include/c++/3.2/bits/ostream.tcc:348:
std::basic_ostream<CharT, _Traits>& std::basic_ostream<CharT,
_Traits>::operator<<(const void*) [with _CharT = char, _Traits =
std::char_traits<char>] /usr/include/c++/3.2/bits/ostream.tcc:120:
std::basic_ostream<CharT, _Traits>& std::basic_ostream<CharT,
_Traits>::operator<<(std::basic_streambuf<CharT, _Traits>*) [with
_CharT = char, _Traits = std::char_traits<char>]
/usr/include/c++/3.2/ostream:211: std::basic_ostream<CharT,
_Traits>& std::operator<<(std::basic_ostream<CharT, _Traits>&,
char) [with _CharT = char, _Traits = std::char_traits<char>]
/usr/include/c++/3.2/bits/ostream.tcc:500: std::basic_ostream<char,
_Traits>& std::operator<<(std::basic_ostream<char, _Traits>&, char)
[with _Traits = std::char_traits<char>]
/usr/include/c++/3.2/ostream:222: std::basic_ostream<char,
_Traits>& std::operator<<(std::basic_ostream<char, _Traits>&,
signed char) [with _Traits = std::char_traits<char>]
/usr/include/c++/3.2/ostream:227: std::basic_ostream<char,
_Traits>& std::operator<<(std::basic_ostream<char, _Traits>&,
unsigned char) [with _Traits = std::char_traits<char>]
/usr/include/c++/3.2/bits/ostream.tcc:572:
std::basic_ostream<CharT, _Traits>&
std::operator<<(std::basic_ostream<CharT, _Traits>&, const char*)
[with _CharT = char, _Traits = std::char_traits<char>]
/usr/include/c++/3.2/bits/ostream.tcc:622: std::basic_ostream<char,
_Traits>& std::operator<<(std::basic_ostream<char, _Traits>&, const
char*) [with _Traits = std::char_traits<char>]
/usr/include/c++/3.2/ostream:246: std::basic_ostream<char,
_Traits>& std::operator<<(std::basic_ostream<char, _Traits>&, const
signed char*) [with _Traits = std::char_traits<char>]
/usr/include/c++/3.2/ostream:251: std::basic_ostream<char,
_Traits>& std::operator<<(std::basic_ostream<char, _Traits>&, const
unsigned char*) [with _Traits = std::char_traits<char>]
```

```
#include <iostream>
#include <algorithm>
#include <iterator>
#include <vector>
class A {};
```

```
int main() {
    std::vector<A> a;
    // ...
    std::copy(a.begin(), a.end(),
        std::ostream_iterator<A>(std::cout,
        "\n"));
}
```

What is wrong here?

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University of Washington by Andrew Lumsdaine

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Organizing template files

```
// min.hpp
#ifndef MIN_HPP
#define MIN_HPP
template <class T> T min(const T& a, const T& b);
#endif // MIN_HPP

// min.cpp
#include "min.hpp"
template <class T>
T min(const T& a, const T& b) { return a < b ? a : b; }

// main.cpp
#include "min.hpp"
int main(int, char* []) {
    return min(0, 1);
}
```

Traditional organization

```
$ g++ -c min.cpp
$ g++ -c main.cpp
$ g++ min.o main.o
main.o: In function 'main':
main.o(.text+0x2a):
undefined reference to 'int min<int>(int const&, int const&)'
collect2: ld returned 1 exit status
```

- `min<int>` has not been instantiated. Why not?

Inclusion model

```
// min.hpp
#ifndef MIN_HPP
#define MIN_HPP
template <class T> T min(const T& a, const T& b) {
    return a < b ? a : b;
}
#endif // MIN_HPP

// main.cpp
#include "min.hpp"
int main(int, char* []) {
    return min(0, 1);
}
```

All source has to be included

Interface Specification

- Lets formalize what we just did
- What does the interface really consist of?
- Operations supported by the parameterized type
- Other types associated with the parameterized type
- Semantics, complexity guarantees
- This set of requirements is called a *concept*
- A type meeting the requirements of a concept is said to *model* the concept

Concepts in Generic Programming

- Generic programming is sometimes called “programming with concepts”
- Syntax
 - Valid expressions
 - Associated types
- Semantics
- Complexity

Iterator Concepts

- In our example, the iterator required `*`, `++`, `!=`
- These are requirements for an InputIterator
- C++ SL has a number of other iterator concepts
- The name of the required concept is usually indicated by the template name

C++ SL Iterator Concepts

- Trivial Iterator: *
- Input Iterator: *, ++
- Output Iterator: *, ++
- Forward Iterator: *, ++
- Bidirectional Iterator: *, ++, --
- Random Access Iterator: *, ++, --, []

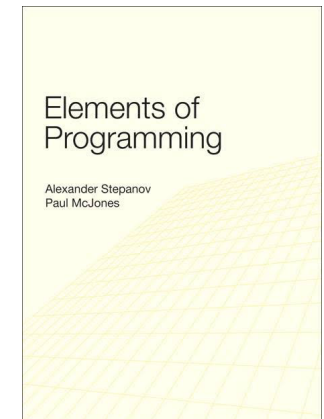
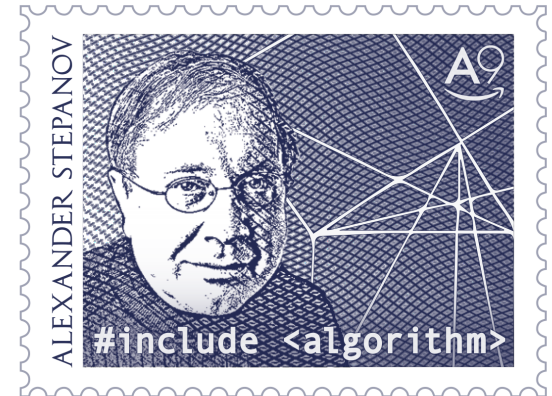
The Standard Template Library

- In early-mid 90s Stepanov, Musser, Lee applied principles of **generic programming** to C++
- Leveraged templates / parametric polymorphism

```
std::set  
std::list  
std::map  
std::vector  
...
```

```
ForwardIterator  
ReverseIterator  
RandomAccessIterator
```

```
std::for_each  
std::sort  
std::accumulate  
std::min_element  
...
```



Alexander Stepanov and Paul McJones. 2009. *Elements of Programming* (1st ed.). Addison-Wesley Professional.

Generic Programming

- Algorithms are **generic** (parametrically polymorphic)
- Algorithms can be used on **any** type that meets algorithmic reqts
 - Valid expressions, associated types
 - Not just std. ::types

Standard Library container

```
vector<double> array(N);
```

```
...
```

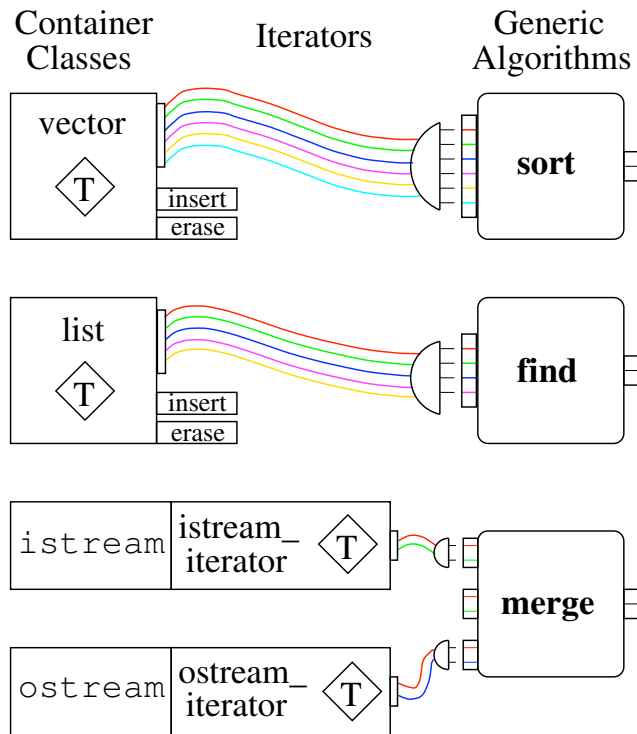
```
std::accumulate(array.begin(), array.end(), 0.0);
```

iterator

iterator

Initial value

Algorithms and data structures connected by iterators



++ **Increment** ==, & **Compare, Reference**
 = **Assign** -- **Decrement**
 * **Dereference** +, -, < **Random Access**

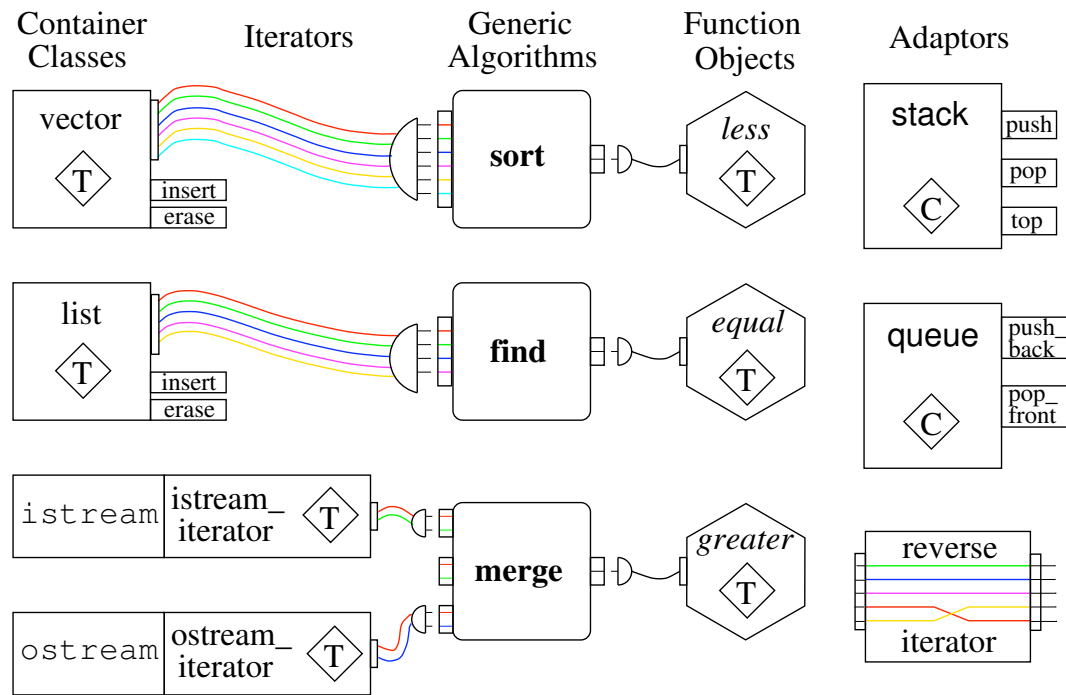
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Five of the six major STL components



++ Increment ==, & Compare, Reference
= Assign -- Decrement
*** Dereference** +, -, < Random Access

◇ Generic Parameter

std Containers

- Note that all containers have **same** interface
- (Actually a hierarchy, we'll come back to this)
- We will primarily be focusing on vector

Headers		<u><vector></u>	<u><deque></u>	<u><list></u>
Members		<u>vector</u>	<u>deque</u>	<u>list</u>
	constructor	<u>vector</u>	<u>deque</u>	<u>list</u>
	operator=	<u>operator=</u>	<u>operator=</u>	<u>operator=</u>
iterators	begin	<u>begin</u>	<u>begin</u>	<u>begin</u>
	end	<u>end</u>	<u>end</u>	<u>end</u>
capacity	size	<u>size</u>	<u>size</u>	<u>size</u>
	max_size	<u>max_size</u>	<u>max_size</u>	<u>max_size</u>
	empty	<u>empty</u>	<u>empty</u>	<u>empty</u>
	resize	<u>resize</u>	<u>resize</u>	<u>resize</u>
element access	front	<u>front</u>	<u>front</u>	<u>front</u>
	back	<u>back</u>	<u>back</u>	<u>back</u>
	operator[]	<u>operator[]</u>	<u>operator[]</u>	
modifiers	insert	<u>insert</u>	<u>insert</u>	<u>insert</u>
	erase	<u>erase</u>	<u>erase</u>	<u>erase</u>
	push_back	<u>push_back</u>	<u>push_back</u>	<u>push_back</u>
	pop_back	<u>pop_back</u>	<u>pop_back</u>	<u>pop_back</u>
	swap	<u>swap</u>	<u>swap</u>	<u>swap</u>

std Containers

- std containers “contain” elements

```
vector<double> array(N);
```

vector of doubles

```
vector<int> array(N);
```

vector of ints

```
list<vector<complex<double> > > thing;
```

list of vectors of complex doubles

- Implementation of list, vector, complex is the same regardless of what is being contained

Generic Programming

- Algorithms are **generic** (parametrically polymorphic)
- Algorithms can be used on **any** type that meets algorithmic reqts
 - Valid expressions, associated types
 - Not just std. ::types

Standard Library container

```
list<vector<complex<double>>> thing(N);
```

...

```
std::accumulate(thing.begin(), thing.end(), 0.0);
```

iterator

iterator

Initial value

std Containers

- The std containers are **class templates** (not “template classes”)

```
template <typename T> class vector;  
template <typename T> class deque;  
template <typename T> class list;
```

What follows is
a template

The template
parameter is a
type placeholder

A class
template

- Don't need details for now

```
vector<double>
```

Example

```
#include <iostream>
#include <algorithm>
#include <vector>
#include <numeric>

int main() {

    std::vector<int> x(10);
    std::iota(x.begin(), x.end(), 0);
    std::copy(x.begin(), x.end(),
              std::ostream_iterator<int>(std::cout, "\n"));

    return 0;
}
```

```
$ g++ copy_print_vector.cpp
$ ./a.out
0
1
2
3
4
5
6
7
8
9
```

Class templates

What is the first rule?

```
template <typename T>
class Vector {
public:
    Vector(size_t M) : num_rows_(M), storage_(num_rows_) {}

    double& operator()(size_t i)      { return storage_[i]; }
    const double& operator()(size_t i) const { return storage_[i]; }

    size_t num_rows() const { return num_rows_; }

private:
    size_t      num_rows_;
    std::vector<T> storage_;
};
```

```
Vector<double> av(10);
```

Thank you!

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